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# SURFACE FRICTION IN OPEN CHANNEL 

## BIRENDRA KUMAR SINGH \& ANAND KUMAR SINHA

Department of Civil Engineering, Birla Institute of Technology, Mesra, Ranchi, Jharkhand, India


#### Abstract

Roughness depends upon size of the roughness material. Since $D_{50}$ are more for 2.5 inch roughness bed as compared to 2.0 inch roughness bed hence lesser value of $\frac{d}{D_{50}}$ and $\frac{d}{D_{84}}$ indicate more roughness. There is less size of 2.0 inch roughness bed which is not submerged as compared to 2.5 inch roughness bed and function of effective roughness concentration depends upon wetted frontal cross sectional area i.e. wetted frontal cross sectional area is more for 2.0 inch roughness bed hence function of effective roughness concentration is more for 2.0 inch roughness bed as compared to 2.5 inch roughness.


Subject Headings: Boulders, Channels, Drag, Flow resistance, Flumes
KEYWORDS: Friction Factor, Hydraulic Geometry, Roughness

## INTRODUCTION

For large scale roughness $\frac{d}{D_{50}}<2$ and $\frac{d}{D_{84}}<1.2$ where d is the mean depth of flow and $\mathrm{D}_{50}=$ the size of the median axis which is bigger than or equal to $50 \%$ of median axis. Similarly $\mathrm{D}_{84}=$ The size of the median axis which is bigger than or equal to $84 \%$ of median axis. Similarly for Intermediate Scale roughness $2<\frac{d}{D_{50}}<7.5$ and $1.2<\frac{d}{D_{84}}$ <4. Hence both the roughness bed provide large scale roughness.

Experimental Set up and Procedures: Data were obtained for 2.0 inch and 2.5 inch roughness bed.
Flume: The flume is open and 1.168 m wide and 9.54 m long. Each roughness bed was constructed by smearing masonite boards with fiberglass resin. The boards were then screwed to the bed of the flume.

Experimental Procedure: For each bed, five to seven flows were measured for three different slopes ( 2,5 and $8 \%$ ). At each flow, depth was gaged at a single cross section, so that mean flow and channel properties could be calculated. In flow with large- scale roughness, the cross- sectional area of flow is significantly affected by the projections of the elements into the flow.

Table 1: Flume Data for 2.0 Inch Roughness Bed

| Sl. No. <br> (1) | Channel <br> Slope (2) | Discharge in <br> Cubic Meters <br> per Second (3) | Mean Velocity <br> in Meters per <br> Second (4) | Mean Depth d <br> in Meters (5) |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 0.02 | 0.00329 | 0.100 | 0.0282 |
| 2 | 0.02 | 0.00837 | 0.189 | 0.0378 |
| 3 | 0.02 | 0.01158 | 0.227 | 0.0436 |


| Table 1: Contd., |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 4 | 0.02 | 0.02541 | 0.377 | 0.0578 |
| 5 | 0.02 | 0.04047 | 0.519 | 0.0668 |
| 6 | 0.02 | 0.04949 | 0.601 | 0.0705 |
| 7 | 0.05 | 0.00329 | 0.132 | 0.0213 |
| 8 | 0.05 | 0.00713 | 0.214 | 0.0285 |
| 9 | 0.05 | 0.01413 | 0.337 | 0.0359 |
| 10 | 0.05 | 0.02068 | 0.431 | 0.0411 |
| 11 | 0.05 | 0.02941 | 0.542 | 0.0465 |
| 12 | 0.05 | 0.04368 | 0.643 | 0.0582 |
| 13 | 0.08 | 0.00247 | 0.162 | 0.0130 |
| 14 | 0.08 | 0.00565 | 0.205 | 0.0236 |
| 15 | 0.08 | 0.01077 | 0.313 | 0.0295 |
| 16 | 0.08 | 0.02187 | 0.515 | 0.0363 |
| 17 | 0.08 | 0.03249 | 0.637 | 0.0437 |
| 18 | 0.08 | 0.03724 | 0.712 | 0.0488 |

Table 2: Flume Data for 2.0 Inch Roughness Bed

| SI. No. <br> $(\mathbf{1})$ | Hydraulic Radius <br> $\mathbf{R}=\frac{W d}{W+2 d}(\mathbf{2})$ | Depth d' of Bed <br> Datum in Meters <br> $(\mathbf{3})$ | Relative <br> Roughness <br> Area $\frac{A w}{W d^{\prime}}(\mathbf{4})$ | Function of <br> Effective <br> Roughness <br> Concentration <br> $(\mathbf{b})(\mathbf{5})$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 0.027 | 0.0505 | 0.4413 | 0.220 |
| 2 | 0.036 | 0.0611 | 0.3814 | 0.281 |
| 3 | 0.041 | 0.0665 | 0.3443 | 0.324 |
| 4 | 0.053 | 0.0795 | 0.2735 | 0.431 |
| 5 | 0.060 | 0.0892 | 0.2511 | 0.483 |
| 6 | 0.063 | 0.0947 | 0.2553 | 0.486 |
| 7 | 0.021 | 0.0442 | 0.5179 | 0.164 |
| 8 | 0.027 | 0.0513 | 0.4450 | 0.218 |
| 9 | 0.034 | 0.0575 | 0.3750 | 0.282 |
| 10 | 0.038 | 0.0633 | 0.3508 | 0.313 |
| 11 | 0.043 | 0.0688 | 0.3252 | 0.348 |
| 12 | 0.053 | 0.0788 | 0.2617 | 0.447 |
| 13 | 0.013 | 0.0411 | 0.6842 | 0.084 |
| 14 | 0.023 | 0.0505 | 0.5330 | 0.161 |
| 15 | 0.028 | 0.0551 | 0.4646 | 0.208 |
| 16 | 0.034 | 0.0659 | 0.4483 | 0231 |
| 17 | 0.041 | 0.0747 | 0.4155 | 0.267 |
| 18 | 0.041 | 0.0701 | 0.3615 | 0.312 |

Table 3: Flume Data for 2.0 Inch Roughness Bed. $D_{50}=\mathbf{0 . 0 4 3 m}, D_{84}=\mathbf{0 . 0 4 7} \mathrm{m}$

| SI. No. <br> $\mathbf{( 1 )}$ | $\frac{d}{D_{50}}$ (2) | $\frac{d}{D_{84}}$ (3) | Manning's <br> Roughness <br> Coefficient $\mathbf{n}$ (4) | Darcy Weisbach <br> Resistance <br> Coefficient f(5) |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 0.656 | 0.600 | 0.186 | 4.463 |
| 2 | 0.879 | 0.804 | 0.120 | 1.654 |
| 3 | 1.014 | 0.928 | 0.109 | 1.323 |
| 4 | 1.344 | 1.230 | 0.078 | 0.639 |
| 5 | 1.553 | 1.421 | 0.061 | 0.390 |
| 6 | 1.640 | 1.500 | 0.055 | 0.307 |
| 7 | 0.495 | 0.453 | 0.190 | 4.796 |
| 8 | 0.663 | 0.606 | 0.139 | 2.437 |
| 9 | 0.835 | 0.764 | 0.103 | 1.245 |
| 10 | 0.956 | 0.874 | 0.087 | 0.870 |

Table 3: Contd.,

| 11 | 1.081 | 0.989 | 0.075 | 0.621 |
| :---: | :---: | :---: | :---: | :---: |
| 12 | 1.353 | 1.238 | 0.073 | 0.553 |
| 13 | 0.302 | 0.277 | 0.141 | 3.092 |
| 14 | 0.549 | 0.502 | 0.164 | 3.522 |
| 15 | 0.686 | 0.628 | 0.123 | 1.892 |
| 16 | 0.844 | 0.772 | 0.085 | 0.860 |
| 17 | 1.016 | 0.930 | 0.078 | 0.676 |
| 18 | 1.042 | 0.853 | 0.070 | 0.554 |

Table 4: Flume Data for 2.0 Inch Roughness Bed

| Sl. No. <br> $\mathbf{( 1 )}$ | Chezy's Resistance Factor c <br> $V$ |
| :---: | :---: |
| 1 | $C=\frac{V}{\sqrt{R S}} \quad(2)$ |
| 2 | 4.303 |
| 3 | 7.044 |
| 4 | 7.927 |
| 5 | 11.579 |
| 6 | 14.892 |
| 7 | 16.931 |
| 8 | 4.074 |
| 9 | 5.824 |
| 10 | 8.173 |
| 11 | 9.888 |
| 12 | 11.689 |
| 13 | 12.491 |
| 14 | 5.023 |
| 15 | 4.779 |
| 16 | 6.613 |
| 17 | 9.875 |
| 18 | 11.123 |

Table 5: Flume Data for 2.5 Inch Roughness Bed

| Sl. No. <br> $(\mathbf{1})$ | Channel <br> Slope (2) | Discharge in <br> Cubic Meters <br> per Second (3) | Mean <br> Velocity in <br> Meters per <br> Second (4) | Mean <br> Depth d in <br> Meters (5) |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 0.02 | 0.00409 | 0.138 | 0.0254 |
| 2 | 0.02 | 0.00993 | 0.223 | 0.0381 |
| 3 | 0.02 | 0.01671 | 0.301 | 0.0475 |
| 4 | 0.02 | 0.02799 | 0.409 | 0.0586 |
| 5 | 0.02 | 0.04110 | 0.500 | 0.0703 |
| 6 | 0.02 | 0.04967 | 0.543 | 0.0782 |
| 7 | 0.05 | 0.00369 | 0.173 | 0.0183 |
| 8 | 0.05 | 0.00855 | 0.283 | 0.0259 |
| 9 | 0.05 | 0.01282 | 0.342 | 0.0321 |
| 10 | 0.05 | 0.02176 | 0.478 | 0.0390 |
| 11 | 0.05 | 0.03403 | 0.611 | 0.0477 |
| 12 | 0.05 | 0.04896 | 0.725 | 0.0578 |
| 13 | 0.08 | 0.00397 | 0.210 | 0.0162 |
| 14 | 0.08 | 0.00605 | 0.259 | 0.0200 |
| 15 | 0.08 | 0.01128 | 0.374 | 0.0258 |
| 16 | 0.08 | 0.01775 | 0.474 | 0.0321 |
| 17 | 0.08 | 0.02737 | 0.592 | 0.0396 |
| 18 | 0.08 | 0.03319 | 0.669 | 0.0425 |
| 19 | 0.08 | 0.04485 | 0.775 | 0.0495 |

Table 6: Flume Data for 2.5 Inch Roughness Bed

| S. No. No <br> $(\mathbf{1})$ | Manning's <br> Roughness <br> Coefficient n(2) | Hydraulic <br> Radius <br> $W d$ <br> $W+2 d$ <br> Meters (3) | Darcy <br> Weisbach <br> Resistance <br> Coefficient f <br> $\mathbf{( 4 )}$ | Chezy's <br> Resistance <br> Factor C <br> $\mathbf{( 5 )}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 0.128 | 0.025 | 2.111 | 6.172 |
| 2 | 0.102 | 0.036 | 1.201 | 8.311 |
| 3 | 0.086 | 0.044 | 0.824 | 10.147 |
| 4 | 0.072 | 0.053 | 0.551 | 12.562 |
| 5 | 0.066 | 0.063 | 0.441 | 14.086 |
| 6 | 0.065 | 0.069 | 0.416 | 14.617 |
| 7 | 0.125 | 0.017 | 2.399 | 5.934 |
| 8 | 0.100 | 0.025 | 1.268 | 8.004 |
| 9 | 0.093 | 0.030 | 1.080 | 8.830 |
| 10 | 0.077 | 0.037 | 0.669 | 11.113 |
| 11 | 0.067 | 0.044 | 0.501 | 13.027 |
| 12 | 0.064 | 0.053 | 0.432 | 14.084 |
| 13 | 0.127 | 0.016 | 2.309 | 5.870 |
| 14 | 0.114 | 0.019 | 1.863 | 6.643 |
| 15 | 0.095 | 0.025 | 1.159 | 8.363 |
| 16 | 0.085 | 0.030 | 0.896 | 9.675 |
| 17 | 0.078 | 0.037 | 0.709 | 10.881 |
| 18 | 0.073 | 0.040 | 0.596 | 11.826 |
| 19 | 0.069 | 0.046 | 0.518 | 12.775 |

Table 7: Flume Data for 2.5 Inch Roughness Bed. $D_{50}=\mathbf{0 . 0 5 4 2 5 m}, D_{84}=\mathbf{0 . 0 5 8 m}$

| S. No. No. <br> (1) | $\frac{d}{D_{50}}$ (2) | $\frac{d}{D_{84}}$ (3) | Depth of Bed <br> Datum d' in <br> Meters (4) | Relative <br> Roughness Area <br> $\frac{A_{w}}{W d^{\prime}}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 0.468 | 0.438 | 0.0567 | 0.5513 |
| 2 | 0.0702 | 0.657 | 0.0691 | 0.4489 |
| 3 | 0.876 | 0.819 | 0.0777 | 0.3879 |
| 4 | 1.080 | 1.010 | 0.0898 | 0.3469 |
| 5 | 1.296 | 1.212 | 0.1007 | 0.3021 |
| 6 | 1.441 | 1.348 | 0.1081 | 0.2761 |
| 7 | 0.337 | 0.316 | 0.0489 | 0.6266 |
| 8 | 0.477 | 0.477 | 0.0585 | 0.5575 |
| 9 | 0.592 | 0.553 | 0.0635 | 0.4942 |
| 10 | 0.719 | 0.672 | 0.0707 | 0.4490 |
| 11 | 0.879 | 0.822 | 0.0799 | 0.4034 |
| 12 | 1.065 | 0.977 | 0.0889 | 0.3497 |
| 13 | 0.299 | 0.279 | 0.0463 | 0.6503 |
| 14 | 0.369 | 0.345 | 0.0517 | 0.6141 |
| 15 | 0.476 | 0.445 | 0.0375 | 0.5512 |
| 16 | 0.592 | 0.553 | 0.0630 | 0.4911 |
| 17 | 0.730 | 0.683 | 0.0705 | 0.4383 |
| 18 | 0.783 | 0.733 | 0.0740 | 0.4265 |
| 19 | 0.912 | 0.853 | 0.0810 | 0.3587 |

Table 8: Flume Data for 2.5 Inch Roughness Bed

| SI. No. <br> (1) | Function of Effective <br> Roughness <br> Concentration (b) (2) |
| :---: | :---: |
| 1 | 0.156 |
| 2 | 0.234 |
| 3 | 0.295 |
| 4 | 0.354 |
| 5 | 0.426 |
| 6 | 0.476 |
| 7 | 0.112 |
| 8 | 0.154 |
| 9 | 0.196 |
| 10 | 0.236 |
| 11 | 0.284 |
| 12 | 0.349 |
| 13 | 0.101 |
| 14 | 0.120 |
| 15 | 0.156 |
| 16 | 0.198 |
| 17 | 0.244 |
| 18 | 0.257 |
| 19 | 0.299 |



Figure 1: Variation of Parameter Mean Velocity of Flow (V) with Parameter Manning's Roughness Coefficient (n) for 2.0 Inch Roughness Bed


Figure 2: Variation of Parameter Function of Effective Roughness Concentration (b) with Parameter Darcy Weisbach Resistance Coefficient (f) for 2.0 Inch Roughness Bed


Figure 3: Variation of Parameter Mean Velocity of Flow (V) with Parameter Chezy's Roughness Coefficient (c) for 2.0 Inch Roughness Bed


Figure 4: Variation of Parameter Darcy Weisbach Resistance Coefficient (f) with Parameter $\frac{d}{D_{50}} \quad$ for 2.0 Inch Roughness Bed

### 2.0 INCH ROUGHNESS BED

i) Average $\quad \frac{d}{D_{50}} \quad=\quad 0.939$
ii) Average $\quad \frac{d}{D_{84}} \quad=\quad 0.859$

| iii) Average discharge of flow | $=0.0218 \mathrm{~m}^{3} / \mathrm{sec}$. |
| :--- | :--- | :--- |
| $\mathrm{D}_{50}=0.043$ meter, $\mathrm{D}_{84}$ | $=0.047$ meter |

### 2.5 INCH ROUGHNESS BED

i) Average $\quad \frac{d}{D_{50}} \quad=\quad 0.742$

| ii) Average $\frac{d}{D_{84}}$ | $=0.694$ |  |
| :--- | :--- | :--- |
| iii) Average discharge of flow | $=$ | $0.0023 \mathrm{~m}^{3} / \mathrm{sec}$. |
| $\mathrm{D}_{50}=0.05425$ meter, $\mathrm{D}_{84}$ | $=0.058$ meter |  |

Roughness depends upon size of the roughness material since $D_{50}$ and $D_{84}$ are more for 2.5 inch roughness bed as compared to 2.0 inch roughness bed hence lesser value of $\frac{d}{D_{50}}$ and $\frac{d}{D_{84}}$ indicate more roughness. There is 1.265 times more roughness for 2.5 inch roughness bed as compared to 2.0 inch roughness bed with respect to $\frac{d}{D_{50}}$. There is 1.238 times more roughness for 2.5 inch roughness bed as compared to 2.0 inch roughness bed with respect to $\frac{d}{D_{84}}$. Since size of the roughness material with respect to $\mathrm{D}_{50}$ is lesser than $\mathrm{D}_{84}$ hence roughness is more for 2.5 inch roughness bed with respect to $\frac{d}{D_{50}}$ as compared to $\frac{d}{D_{84}}$.

Roughness depends upon $\frac{d}{D_{50}}$ and $\frac{d}{D_{84}}$. For large scale roughness $\frac{d}{D_{50}}<2$ and $\frac{d}{D_{84}}<1.2$ where d is the mean depth of flow and $\mathrm{D}_{50}=$ the size of the median axis which is bigger than or equal to $50 \%$ of median axis. Similarly $\mathrm{D}_{84}=$ The size of the median axis which is bigger than or equal to $84 \%$ of median axis. Similarly for Intermediate Scale roughness $2<\frac{d}{D_{50}}<7.5$ and $1.2<\frac{d}{D_{84}}<4$. Hence both the roughness bed provide large scale roughness.

There is 1.023 times more discharge of flow for 2.5 inch roughness bed as compared to 2.0 inch roughness bed hence capacity of the channel is more for large size of roughness material.

Average value of function of effective roughness concentration b for 2.0 inch roughness bed $=0.292$ and average value of function of effective roughness concentration for 2.5 inch roughness bed $=0.245$.

Since size of 2.5 inch roughness material is more as compared to 2.0 inch roughness bed hence it obstructs the flow more and wetted frontal cross sectional area is less due to more size of roughness material hence function of effective roughness concentration is lesser for 2.5 inch roughness bed hence more size of roughness material is more useful to resist more velocity of flow hence destruction is prevented.

As Manning's roughness coefficient (n) increases the function of effective roughness concentration (b) decreases since due to increase in $n$ the mean velocity of flow decreases and roughness is not dominant in lesser velocity of flow hence there is no much rise of water hence less wetted frontal cross sectional area hence b decreases.

Similarly as $f$ increases the $b$ decrease since due to increase in $f$ the mean velocity of flow decrease and roughness is not dominant in lesser velocity of flow hence there is no much rise of water hence less wetted frontal cross sectional area hence $b$ decreases.

We get $d_{\text {max }}$ for the value of $b=0.486$ in 2.0 inch roughness bed whereas at $b=0.476$ we get $d_{\text {max }}$ in 2.5 inch roughness bed. Also $\mathrm{Q}_{\text {max }}$ is obtained for these values of b for 2.0 inch roughness bed and 2.5 inch roughness bed. So these
are the specific values of $b$ to get $d_{\text {max }} \& Q_{\text {max }}$. At lesser value of $b$ we get $d_{\text {max }} \& Q_{\text {max }}$ for 2.5 inch roughness bed that is velocity of flow is much reduced due to larger size of roughness material and depth of flow is more and capacity of the channel is increased. So $b=0.476$ will be effective value since we get more depth of flow \& more discharge of flow.

As chezy's resistance factor increases it means velocity of flow increases because chezy's resistance factor (c) depends upon velocity of flow $(\mathrm{V})$ since $\mathrm{V}=\mathrm{C} \sqrt{ } R S$. As V increases the roughness is more effective hence there is increase in depth of flow hence more wetted frontal cross sectional area is obtained hence as C increases b increases.

As C increases V increases since C depends upon V. Since resistance factor is more effective in high velocity of flow hence as C increases V increases.

Since mean depth of flow is more for 2.0 inch roughness bed as compared to its size with respect to 2.5 inch roughness bed hence we get more wetted frontal cross sectional area for 2.0 inch roughness bed hence function of effective roughness concentration is more for 2.0 inch roughness bed as compared to 2.5 inch roughness bed. There is 1.192 times more function of effective roughness concentration for 2.0 inch roughness bed as compared to 2.5 inch roughness bed. There is 0.023 m size of roughness material which is not submerged for 2.5 inch roughness material whereas there is 0.0104 m size which is not submerged for 2.0 inch roughness material hence we get more function of effective roughness concentration for 2.0 inch roughness bed since 2.0 inch roughness material $=0.0508 \mathrm{~m}$ and mean depth of flow $=0.0404 \mathrm{~m}$ whereas the size for 2.5 inch roughness material $=0.0635 \mathrm{~m}$ and mean depth of flow $=0.0402$ meter.

| Average value of b | $=$ | 0.292 for 2.0 inch roughness bed. |
| :--- | :--- | :--- |
| Average value of b | $=$ | 0.245 for 2.5 inch roughness bed. |

There is 1.192 times more function of effective roughness concentration (b) for 2.0 inch roughness bed as compared to 2.5 inch roughness be.

As $\frac{d}{D_{50}}$ increases it means roughness decreases since roughness $\frac{d}{D_{50}}$ depends upon size of the roughness material i.e. upon $D_{50}$ and $D_{84}$. Due to increase in size of the roughness material i.e. due to increase in $D_{50} \& D_{84}$ roughness increases hence lesser value of $\frac{d}{D_{50}}$ indicates more roughness. Hence due to increase in $\frac{d}{D_{50}}$ value it indicates lesser roughness hence as $\frac{d}{D_{50}}$ increases the Darcy Weisbach resistance coefficient decreases.

### 2.0 INCH ROUGHNESS BED

Relationship between $\mathrm{Q}_{\max }$ and $\mathrm{b}, \mathrm{n}, \mathrm{f}$ and $\mathrm{c}:-$

$$
\begin{equation*}
\mathrm{Q}_{\max }=1.110(\mathrm{C})^{0.541}-1.664(\mathrm{~b})^{0.601}-0.509(\mathrm{n})^{1.964}-0.185(\mathrm{f})^{5.410}+2.426 \mathrm{Q} \tag{1}
\end{equation*}
$$

Relationship between Q and $\mathrm{b}, \mathrm{f}, \mathrm{n}$ and c :-

$$
\begin{equation*}
\mathrm{Q}=0.228(\mathrm{C})^{0.926}-1.072(\mathrm{~b})^{0.933}-0.524(\mathrm{f})^{1.909}-0.806(\mathrm{n})^{1.241}+\frac{Q_{\max }}{2.426} \tag{2}
\end{equation*}
$$

Relationship between d with $\mathrm{b}, \mathrm{f}, \mathrm{n}$ and c :
$\mathrm{d}=0.228(\mathrm{C})^{0.926}-1.072(\mathrm{~b})^{0.933}-0.524(\mathrm{f})^{1.909}-0.806(\mathrm{n})^{1.241}+\frac{d_{\max }}{1.745}$
Relationship for V with $\mathrm{b}, \mathrm{n}, \mathrm{f}$ and c :-
$\mathrm{V}=0.902(\mathrm{C})^{0.385}-1.476(\mathrm{~b})^{0.677}-0.722(\mathrm{n})^{1.385}-0.385(\mathrm{f})^{2.599}+\frac{V_{\max }}{1.869}$

Relationship for $\mathrm{V}_{\text {min }}$ with $\mathrm{b}, \mathrm{f}, \mathrm{n}$ and c :
$\mathrm{V}_{\text {min }}=0.035(\mathrm{C})^{2.127}-0.753(\mathrm{~b})^{1.327}-2.687(\mathrm{f})^{0.372}-1.722(\mathrm{n})^{0.581}+\frac{V_{\text {max }}}{7.120}$

Relationship between $\mathrm{Q}_{\text {max }}$ with $\mathrm{b}, \mathrm{n}$ and f :
$\mathrm{Q}_{\max }=0.051(\mathrm{f})^{5.410}-0.509(\mathrm{n})^{1.964}-1.664(\mathrm{~b})^{0.601}+2.426 \mathrm{Q}$
Relationship between n and f :
$\mathrm{n}=0.057(\mathrm{f})^{1.255}$
Relationship between b and n :-
$\mathrm{b}=21.627(\mathrm{n})^{0.900}$
Relationship between b and c :
$\mathrm{b}=0.016(\mathrm{c})^{1.299}$

We know,
$\mathrm{Q}_{\max }=1.110(\mathrm{c})^{0.541}-1.664(\mathrm{~b})^{0.601}-0.509(\mathrm{n})^{1.964}-0.185(\mathrm{f})^{5.410}+2.426 \mathrm{Q}$
and
$\mathrm{Q}_{\max }=0.051(\mathrm{f})^{5.410}-0.509(\mathrm{n})^{1.964}-1.664(\mathrm{~b})^{0.601}+2.426 \mathrm{Q}$
From $1 \& 2$,
$1.110(\mathrm{c})^{0.541}-1.664(\mathrm{~b})^{0.601}-0.509(\mathrm{n})^{1.964}-0.185(\mathrm{f})^{5.410}$
$=\quad 0.051(\mathrm{f})^{5.410}-0.509(\mathrm{n})^{1.964}-1.664(\mathrm{~b})^{0.601}$
From (9),
(c) ${ }^{1.299}=\frac{6}{0.016}=\frac{1}{0.016} \times b=62.5 b$
$C=(62.5 b)^{\frac{1}{1.299}}=(62.5 b)^{0.770}$
$C \quad=\quad 24.145 b^{0.770}$

> Now $1.110 \quad\left[24.145 b^{0.770}\right]^{0.541}$
> $1.110\left[24.145\left(21.627(\mathrm{n})^{0.900}\right)^{0.770}\right]^{0.541}$
> $=1.110\left[24.145\left(10.665 \mathrm{n}^{0.7623}\right)\right]^{0.541}$
> $=1.110\left[5.600\left(3.599 \mathrm{n}^{0.412}\right)\right]$
> $=1.110\left[20.154 \mathrm{n}^{0.412}\right]$
> $=22.371 \mathrm{n}^{0.412}$
> $1.664(\mathrm{~b})^{0.601}=1.664\left[21.627(\mathrm{n})^{0.900}\right]$
> $=\quad 1.662\left[6.344(\mathrm{n})^{0.541}\right]$
> $=\quad 10.556 \mathrm{n}^{0.541}$
> $0.185(\mathrm{f})^{5.410}=0.185\left[9.808 \mathrm{n}^{0.797}\right]^{5.410}$
> $=0.185\left[231446.32 \mathrm{n}^{4.312}\right]$
> $=\quad 42817.57 \mathrm{n}^{4.312}$
> $0.051(\mathrm{f})^{5.410}=0.051\left[9.809 \mathrm{n}^{0.797}\right]^{5.410}$
> $=\quad 0.051\left[231446.32 \mathrm{n}^{4.312}\right]$
> $=\quad 11803.76 n^{4.312}$
> $1.664(b)^{0.601}=1.664\left[21.627(\mathrm{n})^{0.900}\right]^{0.601}$
> $=\quad 1.664\left[6.344 \mathrm{n}^{0.541}\right]$
> $=\quad 1.556 \mathrm{n}^{0.541}$

Now,
$22.371 n^{0.412}-42817.57 n^{4.312}$

$$
\begin{aligned}
& = \\
& 11.803 .76 \mathrm{n}^{4.312} \\
22.371 \mathrm{n}^{0.412} & =11803.76 \mathrm{n}^{4.312}+42817.57 \mathrm{n}^{4.312} \\
& =\quad 54621.33 \mathrm{n}^{4.312}
\end{aligned}
$$

$\frac{5421.33 n^{4.312}}{22.371 n^{0.412}}=1$
Or $2.42 .34 \mathrm{n}^{4.312-0.412}=1$
Or $n^{3.900}=\frac{1}{242.34}=0.0041$
$\therefore \mathrm{n} \quad=\quad(0.0041)^{\frac{1}{3.900}}$

$$
=\quad(0.0041)^{0.256} \quad=\quad 0.245 \approx 0.108
$$

## Mathematical Formulation for Q

$$
\begin{align*}
& \mathrm{Q}_{\max }=1.110(\mathrm{c})^{0.541}-1.664(\mathrm{~b})^{0.601}-0.509(\mathrm{n})^{1.964}-0.185(\mathrm{f})^{5.410}+2.426 \mathrm{Q}  \tag{1}\\
& \mathrm{Q}=0.228(\mathrm{c})^{0.926}-1.072(\mathrm{~b})^{0.933}-0.524(\mathrm{f})^{1.909}-0.806(\mathrm{n})^{1.241}+\frac{Q_{\max }}{2.426} \tag{2}
\end{align*}
$$

Substituting $\mathrm{Q}_{\text {max }}$ from 1 in 2

$$
\mathrm{Q}=0.228(\mathrm{c})^{0.926}-1.072(\mathrm{~b})^{0.933}-0.524(\mathrm{f})^{1.909}-0.806(\mathrm{n})^{1.241}+\frac{1}{2.426} \quad\left[1.110(\mathrm{c})^{0.541}-1.664(\mathrm{~b})^{0.601}-0.509(\mathrm{n})^{1.964}-\right.
$$

$$
\left.0.185(\mathrm{f})^{5.410}+2.426 \mathrm{Q}\right]
$$

$$
=\quad 0.228\left[24.145(\mathrm{~b})^{0.770}\right]^{0.926}-1.072(\mathrm{~b})^{0.933}-0.524(\mathrm{f})^{1.909}-0.806\left[0.057(\mathrm{f})^{1.255}\right]^{1.241}+\frac{1}{2.426} \quad[1.110 \quad(24.145
$$

$\left.\left.\left.(b)^{0.770}\right)^{0.541}\right]-1.664(b)^{0.601}-0.509\left(0.057(\mathrm{f})^{1.255}\right)^{1.964}-0.185(\mathrm{f})^{5.410}+2.426 \mathrm{Q}\right]$
Substituting the average value of $b, f$, and $Q$ in the above equation we gat:

$$
\mathrm{Q}=0.228\left[19.076(\mathrm{~b})^{0.713}\right]-1.702 \times 0.317-1.3804-0.806\left[0.0286(1.661)^{1.557}\right]+\frac{1}{2.426} \quad\left[1.110\left(5.599(0.292)^{0.417}\right)-\right.
$$ $\left.0.794-0.509\left(0.0036(1.661)^{2.465}\right)-2.880+2.426 \mathrm{Q}\right]$

$$
\begin{aligned}
& \mathrm{Q}=1.808-0.340-1.3804-0.0508+\frac{1}{2.426}[3.720-0.794-0.0064-2.880+0.04949] \\
& =0.0728+\frac{1}{2.426}[3.7695-3.6804] \\
& =0.0728+0.0367 \quad=0.110 \approx 0.04949
\end{aligned}
$$

Mathematical formulation for V :

$$
\begin{align*}
& \mathrm{V}=0.902(\mathrm{C})^{0.385}-1.476(\mathrm{~b})^{0.677}-0.722(\mathrm{n})^{1.385}-0.385(\mathrm{f})^{2.599}+\frac{V_{\max }}{1.869}  \tag{1}\\
& \mathrm{~V}_{\min }=0.035(\mathrm{C})^{2.127}-0.753(\mathrm{~b})^{1.327}-2.687(\mathrm{f})^{0.372}-1.722(\mathrm{n})^{0.581}+\frac{V_{\max }}{7.120} \tag{2}
\end{align*}
$$

From (2)

$$
\begin{aligned}
& \left.\frac{V_{\max }}{7.120}=\mathrm{V}_{\min }-0.035(\mathrm{C})^{2.127}+0.753(\mathrm{~b})^{1.327}+2.687(\mathrm{f})^{0.372}+1.722 \mathrm{n}\right)^{0.581} \\
\therefore & \mathrm{~V}_{\max }=7.120\left[\mathrm{~V}_{\min }-0.035(\mathrm{C})^{2.127}+0.753(\mathrm{~b})^{1.327}+2.687(\mathrm{f})^{0.372}+1.722(\mathrm{n})^{0.581}\right] \\
= & 7.120 \mathrm{~V}_{\min }-0.2492(\mathrm{C})^{2.127}+5.361(\mathrm{~b})^{1.327}+19.131(\mathrm{f})^{0.372}+12.261(\mathrm{n})^{0.581}
\end{aligned}
$$

Substituting $V_{\max }$ in (1) we get:

$$
\begin{aligned}
\mathrm{V}=\quad & 0.902(\mathrm{C})^{0.385}-1.476(\mathrm{~b})^{0.677}-0.722(\mathrm{n})^{1.385}-0.385(\mathrm{f})^{2.599}+\frac{1}{1.869} \\
& {\left[7.120 \mathrm{~V}_{\min }-0.249(\mathrm{C})^{2.127}+5.361(\mathrm{~b})^{1.327}+19.131(\mathrm{f})^{0.372}+12.261(\mathrm{n})^{0.581}\right] }
\end{aligned}
$$

Substituting the average values of $\mathrm{c}, \mathrm{b}, \mathrm{n} \& \mathrm{f}$ and $\mathrm{V}_{\text {min }}$ we get:-

$$
\begin{aligned}
& V=0.902(9.153)^{0.385}-1.476(0.292)^{0.677}-0.722(0.108)^{1.385}-0.385(1.661)^{2.599}+\frac{1}{1.869} \\
& {\left[7.120 \times 0.100-0.2492(9.153)^{2.127}+5.361(0.292)^{1.327}+19.131(1.661)^{0.372}+12.261(0.108)^{0.581}\right]} \\
& =2.115-0.641-0.033-1.438+\frac{1}{1.869}[0.712-27.656+1.047+23.105+3.365] \\
& =2.115-2.113+\frac{1}{1.869}[28.229-27.656] \\
& =0.002+0.307=0.309 \mathrm{~m} / \mathrm{sec} \approx 0.381 \mathrm{~m} / \mathrm{sec}
\end{aligned}
$$

Hence this is the required mathematical formulation for V .

## CONCLUSIONS

There is 1.265 times more roughness for 2.5 inch roughness bed as compared to 2.0 inch roughness bed with respect to $\frac{d}{D_{50}}$. There is 1.238 times more roughness for 2.5 inch roughness bed as compared to 2.0 inch roughness bed with respect to $\frac{d}{D_{84}}$. As Manning's roughness coefficient (n) increases the function of effective roughness concentration (b) decreases because due to increase in $n$ velocity of flow decreases and roughness is not so effective in low velocity of flow to raise more depth of flow. Hence wetted frontal cross sectional area is less hence function of effective roughness concentration decreases due to increase in n . As V increases the roughness is more effective hence chezy's resistance factor $\mathrm{C} \&$ function of effective roughness concentration b both increase.

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## APPENDICES: NOTATION

The following symbols are used in this paper:

| $\frac{A_{w}}{W d^{\prime}}$ | $=$ Relative roughness area |
| :--- | :--- |
| $\mathrm{A}_{\mathrm{w}}$ | $=$ Wetted cross sectional area |
| b | $=$ Function of effective roughness concentration |
| C | $=$ Chezy's resistance factor |
| d | $=$ Mean depth of flow in meters |
| d, | $=$ Depth of bed datum in meters. |
| $\mathrm{D}_{50}$ | $=$ The size of median axis which is bigger than or equal to $50 \%$ of median axis. |
| $\mathrm{D}_{84}$ | $=$ The size of median axis which is bigger than or equal to $84 \%$ of median axis. |
| f | $=$ Darcy Weisbach resistance coefficient |
| g | $=$ Acceleration due to gravity |
| n | $=$ Manning's roughness coefficient |
| P | $=$ Wetted Perimeter |
| Q | $=\quad$ Discharge in cubic meters per second |


| R | $=$ Hydraulic radius $=\frac{A}{p}$ |
| :--- | :--- |
| A | $=$ Flow cross sectional area $=\mathrm{Wd}$ |
| P | $=$ Wetted Perimeter |
| S | $=\quad$ Channel slope |
| V | $=\quad$ Mean velocity of flow in meters per second. |
| W | $=\quad$ Width of the channel $=1.168 \mathrm{~m}$ |

## Formula Used

$$
\begin{aligned}
& \frac{A_{w}}{W d^{\prime}}=\left(\frac{w}{d}\right)^{-b} \\
& \begin{array}{l}
\left(\frac{8}{f}\right)^{1 / 2}= \\
\quad=\frac{V}{(g R S)^{1 / 2}} \\
\text { Hydraulic radius } R=\frac{W d}{W+2 d} \\
\mathrm{~V} \\
\mathrm{~V} \\
\mathrm{~V} \\
\mathrm{R} \\
\mathrm{~V} \\
\mathrm{~A}+\mathrm{A}_{\mathrm{w}}
\end{array} \\
& =\quad \frac{A}{P}=\frac{W \sqrt{R S}}{W+2 d} R^{2 / 3} S^{1 / 2} \\
&
\end{aligned}
$$

